

## ERRATA

★ On the Cauchy problem for a class of hyperbolic operators whose coefficients depend only on the time variable, Tsukuba J. Math. 39-1 (2015), 121-163

- p123ℓ7 ↑  $\Gamma(p(t, \cdot) \rightarrow \Gamma(p(t(s), \cdot$
- p123ℓ1 ↑  $h_k(t, \xi) \rightarrow h_k(t, \tau, \xi)$
- p136ℓ3 ↑  $\#\{t \in \rightarrow \{t \in$
- p145ℓ3 ↓  $+\Lambda_t^{-1} \rightarrow -\Lambda_t^{-1}$
- p152ℓ14 ↓  $\mathcal{N}_1^0(p^{(1)}) \rightarrow \mathcal{N}_1^0(p^{(1)})$

### 2022.4.6

- p134ℓ9 ↓  $\equiv 0$ . Write  $\rightarrow$   
 $\equiv 0$ . Since  $d_0(t, \xi; \varepsilon)d_1(t, \xi; \varepsilon) \in \mathcal{A}[\xi, \varepsilon]$ , it follows from Lemma 2.1 that for any  $T > 0$  there is  $N_{T,0} \in \mathbf{Z}_+$  such that

$$\begin{aligned} & \#\{t \in [0, T]; \lambda_j(t, \xi; \varepsilon) - \lambda_k(t, \xi; \varepsilon) = 0\} \\ & (\#\{t \in [0, T]; d_0(t, \xi; \varepsilon)d_1(t, \xi; \varepsilon) = 0\}) \leq N_{T,0} \end{aligned}$$

if  $\varepsilon \in \mathbf{R} \setminus \mathcal{N}_0^0$ ,  $\xi \in S^{n-1} \setminus \mathcal{N}_0(\varepsilon)$ ,  $1 \leq j < k \leq \hat{m}$  and  $\lambda_j(t, \xi; \varepsilon) - \lambda_k(t, \xi; \varepsilon) \not\equiv 0$  in  $t$ . Write

- p136ℓ8 ↓  $\leq m \rightarrow \leq \hat{m}$

### 2022.4.16

- p141ℓ1 ↑  $+(i/2)\partial_t \rightarrow +(3i/2)\partial_t$
- p154 ℓ3 ↓  $+\text{Im} \rightarrow -\text{Im}$
- p154 ℓ7 ↓  $+\text{Re} \rightarrow -3\text{Re}$
- p154 ℓ8 ↓  $p_1^{(1)}v_\varepsilon \cdot \overline{v_\varepsilon} \rightarrow p_1^{(1)}v_\varepsilon \cdot \overline{v_\varepsilon}/3$
- p154 ℓ3 ↑  $-\sum_{j=1}^3 \rightarrow -\sum_{j=1}^2$
- p154 ℓ2 ↑  $|(\lambda_{2t}^{(1)} - \lambda_{1t}^{(1)})v_\varepsilon|^2/4 \rightarrow 9|(\lambda_{2t}^{(1)} - \lambda_{1t}^{(1)})v_\varepsilon|^2$

- p154 ℓ1 ↑  $W_0^4 \Lambda_t^{-1} \rightarrow W_0^4 \Lambda_t^{-1} e^{-A\Lambda}$

★ On the Cauchy problem for second-order hyperbolic operators with the coefficients of their principal parts depending only on the time variable, Funkcialaj Ekvacioj 55 (2012), 99-136:

- p101ℓ8 ↑  $\Gamma(p(t, \cdot) \rightarrow \Gamma(p(t(s), \cdot)$
- p114ℓ12 ↓  $\psi(t, \xi') \rightarrow \psi_j(t, \xi')$
- p115ℓ7 ↑  $\beta_{2,(t)} \rightarrow \beta_2(t)$
- p128ℓ13 ↑ only in  $\rightarrow$  only if
- p129ℓ11 ↓  $\lambda(s) \rightarrow \lambda_1(s), \lambda(0) \rightarrow \lambda_1(0)$

★ On the Cauchy problem for hyperbolic operators of second order whose coefficients depend only on the time variable, J. Math. Soc. Japan 62-1 (2010), 95-133:

- p96ℓ2 ↓  $\xi_1^{\alpha_1}, \dots, \xi_n^{\alpha_n} \rightarrow \xi_1^{\alpha_1} \dots \xi_n^{\alpha_n}$
- p100ℓ8 ↑ & ℓ6 ↑  $U_{(t_0, x^0)} \rightarrow U_{(t_0, \xi^0)}, \Gamma_{(t_0, x^0)} \rightarrow \Gamma_{(t_0, \xi^0)}$
- p101ℓ3 ↑  $(A-a)(t_0, \xi_0) \rightarrow (A-a)_{(t_0, \xi^0)},$   
 $(A-b)(t_0, x_0, \xi_0) \rightarrow (A-b)_{(t_0, x^0, \xi^0)}$
- p104ℓ1 ↓  $)^2 \rightarrow )^2)$
- p105ℓ3 ↑ & ℓ2 ↑  $T(\theta) \rightarrow (t_0 + T(\theta), \theta)$
- p106ℓ6 ↑ & ℓ5 ↑  $T(\theta) \rightarrow (t_0 + T(\theta), \theta)$
- p110ℓ12 ↓  $\hat{u}_j(x) \rightarrow \hat{u}_j(\xi)$
- p123ℓ9 ↓  $u_j(s_0, y; \rho) = 0 \rightarrow u_0(s_0, y; \rho) = 1$
- p124ℓ8 ↑ functions  $\rightarrow$  functions defined in  $[0, \theta_0]$
- p124ℓ7 ↑  $0 \leq \lambda_1 \rightarrow -t_0 \leq \lambda_1$
- p124ℓ5 ↑  $[0, \theta_0]. \rightarrow (0, \theta_0].$
- p125ℓ8 ↓  $\lambda_1(\theta) > 0, \rightarrow \lambda_1(\theta) > 0$  for  $\theta \in (0, \theta_0]$ ,
- p128ℓ2 ↓  $+(p_j + p)\tilde{\mu} \rightarrow +p\tilde{\mu}$

- p129ℓ1 ↓ ~ ℓ3 ↓ (3 places)  $\mathbf{R}^{n+2} \rightarrow \mathbf{R} \times S^{n-1} \times \mathbf{R}$
- p129ℓ7 ↑ & ℓ3 ↑ ;  $|\xi - \rightarrow ; |\xi|^2 = 1, |\xi -$
- p130ℓ1 ↓ ;  $|\xi - \rightarrow ; |\xi|^2 = 1, |\xi -$
- p130ℓ9 ↑  $\Gamma \rightarrow (\Gamma \cap S^{n-1})$
- p130ℓ7 ↑  $|t - t_k|^2. \rightarrow |t_k - t_0|^2.$
- p131ℓ1 ↓  $\min_{\tau \in \mathcal{R}(\xi)} \rightarrow \min_{\tau \in \mathcal{R}(\tilde{\Xi}(\rho))}$

★ The  $C^\infty$ -well posed Cauchy problem for hyperbolic operators dominated by time functions, Japanese J. Math. 30-2 (2004), 283-348 (with K. Kajitani and K. Yagdjian):

- p316ℓ13 ↑, p317ℓ7 ↓ and p320ℓ5 ↓ Delete “a conic neighborhood of”
- p317ℓ7 ↓  $\chi(\tilde{\mathcal{C}}_2), \rightarrow \chi(\tilde{\mathcal{C}}_2)$  and

★ The Cauchy problem for hyperbolic operators dominated by time functions, Hyperbolic Problems and Related Topics, International Press, 2003, pp423-436:

- p429ℓ16 ↓  $\text{Re } \beta^0(y, 0, \eta') + |\text{Im } \beta^0(y, 0, \eta')|$   
 $\rightarrow \max\{\text{Re } \beta^0(y, 0, \eta'), |\text{Im } \beta^0(y, 0, \eta')|\}$

★ The Cauchy problem for a class of hyperbolic operators with double characteristics, Funkcialaj Ekvacioj 39-2 (1996), 235-307 (with K. Kajitani):

- p238ℓ2 ↓  $e(y, \eta') \rightarrow e(y, \eta)$
- p238ℓ11 ↓  $C_2(y, n') \rightarrow C\alpha(y, \eta')$
- p239ℓ13 ↓ and p240ℓ6 ↓ The term “ $T(y, 0, \eta'')^{-2}\alpha(y, 0, \eta'')/|\eta''|$ ” can be dropped.
- p240ℓ4 ↑ The term “ $C_1\alpha(y, 0, \eta'')^{1/2}$ ” can be dropped.
- p253ℓ11 ↓  $g_j$  temperate in  $\dots$  ( $j = 1, 2$ ).  
 $\rightarrow G$  temperate in  $\dots$  ( $j = 1, 2$ ), where  $G = (g_1 + g_2)/2$ .
- p253ℓ16 ↓  $D''$ ),  $a \cdots a(x, \xi'')$  and  $G = (g_1 \oplus g_2)/2$   
 $\rightarrow D''$ ) and  $a \cdots a(x, \xi'')$ .
- p265ℓ11 ↓  $-e_s(y, \eta) \rightarrow -e_s(y, \eta)$

- p267ℓ15 ↑  $\tilde{d} \rightarrow \tilde{d}_1$

★ Microlocal *a priori* estimates and the Cauchy problem II, Japan. J. Math. 20-1 (1994), 1-71 (with K. Kajitani):

- p12ℓ7 ↑  $\tilde{\mathcal{C}} \ni \rightarrow \chi : \tilde{\mathcal{C}} \ni$
- p12ℓ7 ↑  $(y, \eta) \in \mathcal{C} \rightarrow (x, \xi) \in \mathcal{C}$
- p16ℓ4 ↑  $(2n + 1)! \rightarrow (2n)!$
- p29ℓ8 ↑  $u(w) dy \rightarrow u(w) dw$
- p38ℓ7 ↑  $\Theta_{h/2}(y, \eta) \rightarrow \Theta_{h/2}(\eta)$
- p39ℓ11 ↑  $\mathcal{E}_s(y, \eta; \rightarrow \mathcal{E}_s(y, D;$
- p48ℓ9 ↑  $r(x, D) \rightarrow r(y, D)$
- p61ℓ8 ↓  $\tilde{w}(y, \eta; \gamma)) \rightarrow \tilde{w}(y, \eta; \gamma)\vartheta$

★ Microlocal *a priori* estimates and the Cauchy problem I, Japan. J. Math. 19-2 (1993), 353-418 (with K. Kajitani):

- p354ℓ1 ↓  $\langle \xi' \rangle^{\delta|\beta| - \rho|\alpha'|} \rightarrow \langle \xi' \rangle^{m + \delta|\beta| - \rho|\alpha'|}$
- p354ℓ20 ↑ real-valued  $\rightarrow$  bounded real-valued
- p354ℓ20 ↑  $C^2(\mathcal{C}_2) \rightarrow C^\infty(\mathcal{C}_2)$
- p375ℓ5 ↓ Delete “(3.2)”
- p375ℓ9 ↓  $\|\langle D \rangle \rightarrow (3.2) \|\langle D \rangle$
- p387ℓ7 ↓ taht  $\rightarrow$  that
- p401ℓ10 ↑  $D; \gamma; B) \rightarrow D; \gamma'; B)$
- p407ℓ10 ↓  $\times \tilde{\psi}_\gamma \rightarrow \times \psi_\gamma$
- p407ℓ10 ↑  $\tilde{\mathcal{R}}(x, \xi; \rightarrow \tilde{\mathcal{R}}(x, D;$

★ Propagation of singularities for several classes of pseudodifferential operators, Bull. Sc. math., 2 serie 115 (1991), 397-449 (with K. Kajitani):

- p435ℓ5 ↑  $= \nabla_\xi \Lambda( \rightarrow = \nabla_\xi \varphi($

- p436ℓ11 ↓  $\mathcal{C}_0 \rightarrow \mathcal{C}_0$  of  $z^0$
- p437ℓ10 ↑  $-\mathcal{V}(z) \rightarrow -\tilde{\mathcal{V}}(z)$
- p440ℓ11 ↑  $|\lambda(x, \xi')| \rightarrow |\lambda(x, \xi')|^2$ ,
- The argument from p446ℓ16 ↓ to p447ℓ9 ↓ can be simplified as follows:  
Now assume that  $1 \leq k \leq \ell$  and  $z^0 \notin WF(x_1^k u)$ . Since

$$x_1^{k-1} P(x, D)u = D_1(x_1^k u) + (q(x', D') + ik)(x_1^{k-1} u),$$

we have  $z^0 \notin WF((q(x', D') + ik)(x_1^{k-1} u))$ . The assumptions in Theorem 6.1 implies that  $iq_0(0; 0, \dots, 0, 1) \notin \mathbf{N}$ , *i.e.*,  $q(x', D') + ik$  is elliptic at  $z^0$ . Thus we have  $z^0 \notin WF(x_1^{k-1} u)$ .

★ The hyperbolic mixed problem in Gevrey classes, Japan. J. Math. 15 (1989), 309-383 (with K. Kajitani):

- p313ℓ6 ↓  $([0, \cdot]); \rightarrow ([0, \infty));$
- p319ℓ ↑ that  $r'_0 \geq \rightarrow$  that  $r'_0 \geq$
- p324ℓ2 ↓  $-i\Gamma_{x'} \rightarrow -i\dot{\Gamma}_{x'}$

★ Microhyperbolic operators in Gevrey classes, Publ. RIMS, Kyoto Univ. 25-2 (1989), 169-221 (with K. Kajitani):

- p178ℓ4 ↓  $\delta_1 \oplus \delta_2 \rightarrow \delta_1 + \delta_2$
- p189ℓ8 ↓  $\xi \cdot y, \rightarrow \xi, y,$
- p190ℓ7 ↓ and ℓ12 ↓  $\geq \rightarrow \leq$
- p190ℓ4 ↑  $\cap(\xi \rightarrow \cap\{\xi$
- p191ℓ4 ↓ and ℓ13 ↑  $\phi \rightarrow \emptyset$
- p191ℓ13 ↑  $(\cap \mathcal{C}_2 \rightarrow \cap(\mathcal{C}_2$
- p191ℓ1 ↑  $\equiv \varepsilon_1 \rightarrow \equiv \hat{\varepsilon}_1$
- p193ℓ7 ↑  $c_{d^1} \rightarrow c_{d_1}$
- p194ℓ4 ↓  $(1/p(x, \xi) \rightarrow (1/p(x, \xi))$
- p205ℓ1 ↓  $\mathbf{C}^n. \rightarrow \mathbf{C}^n,$

- p213ℓ13 ↓ taht → that
- p214ℓ15 ↓  $H_{a(\Lambda'_h+bw_h)}^m \rightarrow H_{a(\Lambda'_h+bW_h)}^m$  (two places)
- p216ℓ12 ↓  $(PQf - f \rightarrow (pQf - f$
- p216ℓ2 ↑  $WP_* \rightarrow WF_*$
- p218ℓ12 ↓ tath → that

★ Remarks on hyperbolic polynomials, Tsukuba J. Math. 10-1 (1986), 17-28:

- p18ℓ10 ↓  $X \times \rightarrow U \times \leftarrow$  '06.7.14
- p19ℓ4 ↓  
the  $\alpha_j(b_1, \dots, b_m)$  are continuous functions of  $(b_1, \dots, b_m) \in \mathbf{C}^m$ .  
→  
 $\mathbf{C}^m \ni (b_1, \dots, b_m) \mapsto \{\alpha_1(b_1, \dots, b_m), \dots, \alpha_m(b_1, \dots, b_m)\} \subset \mathbf{C}$  is a  
multi-valued continuous function. ← '06.7.14
- p21ℓ13 ↑ for  $\theta \in [0, 1]$ . →  
for  $\theta \in [0, 1]$ . About the choice of a continuous function  $s(\theta)$  we refer  
to Theorem 5.2 of Chapter II of "T. Kato, Perturbation Theory for  
Linear Operators, Springer-Verlag, Berlin-Heidelberg-New York, 1980"

★ Singularities of solutions of the Cauchy problem for hyperbolic systems in  
Gevrey classes, Japan. J. Math. 11-1 (1985), 131-175:

- p161ℓ4 ↓  $D_x^\beta \partial^\alpha p(x, \xi) \rightarrow D_x^\beta \partial_\xi^\alpha p(x, \xi)$
- p164ℓ3 ↓  $\tilde{L}_{(\mu)}^{(\alpha)} \rightarrow \tilde{L}_{(\beta)}^{(\alpha)}$
- p172ℓ11 ↓ - ℓ16 ↓ →

$$\begin{aligned}
&\leq 2^{-1} \left\{ \sum_{\beta} |D_x^{\alpha+\beta} \psi(x)| |y|^{|\beta|} b_{|\beta|} |\chi'(b_{|\beta|}|y|)| / \beta! \right. \\
&\quad \left. + \sum_{\beta} |D_x^{\alpha+\beta} \partial_{x_j} \psi(x)| |y|^{|\beta|} |\chi(b_{|\beta|}|y|) - \chi(b_{|\beta|+1}|y|)| / \beta! \right\} \\
&\leq C |y|^k A^{|\alpha|} \left\{ \sum_{\beta} (|\alpha| + |\beta|)!^{\kappa_1} A^{|\beta|} (B|y|/h)^{|\beta|-k} b_{|\beta|} (h/B)^{|\beta|-k} \right. \\
&\quad \times |\chi'(b_{|\beta|}|y|)| / \beta! + \sum_{\beta} (|\alpha| + |\beta| + 1)!^{\kappa_1} A^{|\beta|} (B|y|/h)^{|\beta|-k} \\
&\quad \left. \times (h/B)^{|\beta|-k} |\chi(b_{|\beta|}|y|) - \chi(b_{|\beta|+1}|y|)| / \beta! \right\} \\
&\leq C' (B|y|/h)^k (2^{\kappa_1} A)^{|\alpha|} |\alpha|!^{\kappa_1} k!^{\kappa_1-1} \sum_{\beta} \{B|\beta|^{\kappa_1-1} \\
&\quad \times (|\beta|! |\beta|^k / (k! |\beta|^{|\beta|}))^{\kappa_1-1} + (|\beta| + 1)^{\kappa_1-2} \\
&\quad \times ((|\beta| + 1)! (|\beta| + 1)^k / (k! (|\beta| + 1)^{|\beta|+1}))^{\kappa_1-1}\} (2^{\kappa_1+1} n h A / B)^{|\beta|}.
\end{aligned}$$

Since  $|\beta|! |\beta|^k / (k! |\beta|^{|\beta|}) \leq 1$ , taking  $B > 4^{\kappa_1} n h A$ , we have (2.28).  
Q.E.D.

- p174ℓ5 ↑  $(x^0, \xi^0) \in {}^* \mathbf{R}^n \rightarrow (x^0, \xi^0) \in T^* \mathbf{R}^n$

★ The mixed problem for hyperbolic systems, Proc. NATO Advanced Study Institutes on Singularities in boundary value problems, Series C, D. Reidel, 1981, 327-370:

- p365ℓ14 ↑  $\notin WF_0 \rightarrow \in WF_0$

★ The Cauchy problem for operators with constant coefficient hyperbolic principal part and propagation of singularities, Japan. J. Math. 6 (1980), 179-228:

- p180ℓ12 ↑ and ℓ11 ↑  $\mathcal{D}^{\{\kappa\}, h} \rightarrow \mathcal{D}_K^{\{\kappa\}, h}$
- p183ℓ11 ↑  $\varepsilon \leq r_1 \rightarrow \varepsilon \leq \varepsilon_1$
- p185ℓ12 ↓  $\text{supp} \rightarrow \text{sup}$
- p187ℓ12 ↓  $\text{Lemm} \rightarrow \text{Lemma}$
- p189ℓ7 ↓  $q(s) \rightarrow q_0(s)$

- p193ℓ6 ↑ and ℓ3 ↑  $f(\nu, r, \zeta, s, t) \rightarrow f(\nu, r, \zeta, t$
- p209ℓ4 ↑  $(-is^{-\sigma}\zeta) \rightarrow +s^{-\sigma}\zeta) \leftarrow$  '06.7.13

★ Analytic wave front sets of the Riemann functions of hyperbolic mixed problems in a quarter-space, Publ. RIMS, Kyoto Univ. 11-3 (1976), 785-807:

- p785ℓ15 ↑ Garding  $\rightarrow$  Gårding
- p787ℓ6 ↑  $+\Gamma_0 \rightarrow +\Sigma_0$
- p789ℓ1 ↓  $i\Gamma \rightarrow i\dot{\Gamma}$
- p789ℓ3 ↑  $\rightarrow \{\tilde{R}_0(\zeta') = 0\} \cup (-i\partial\dot{\Gamma})\}$ .
- p790ℓ7 ↓  $\Sigma \rightarrow \dot{\Sigma}$

★ The principle of limit amplitude for symmetric hyperbolic systems of first order in the half-space  $\mathbf{R}_+^n$ , Publ. RIMS, Kyoto Univ. 11-1 (1975), 149-162:

- p161ℓ1 ↓  $f(x) dx \rightarrow h(x) dx$